

Problem 1. Given $\triangle ABC$ with vertices at $A(0,0), B(b,0), C(a,h)$ with all a, b, h positive real numbers. Let M_1 be the mid point of segment BC , M_2 be the midpoint of segment AM_1 , M_3 be the mid point of BM_2 , ..., M_{2k} be the mid point of AM_{2k-1} and M_{2k+1} be the mid point of BM_{2k} for $k = 1, 2, \dots$. Show that the evenly indexed mid-points converge to the point on segment AB which is one-third away from vertex A and the oddly-indexed mid-points converge to a point on side AB which is two-third away from vertex A . Precisely $M_{2k} \rightarrow \left(\frac{b}{3}, 0\right)$ and $M_{2k+1} \rightarrow \left(\frac{2b}{3}, 0\right)$ as $k \rightarrow \infty$